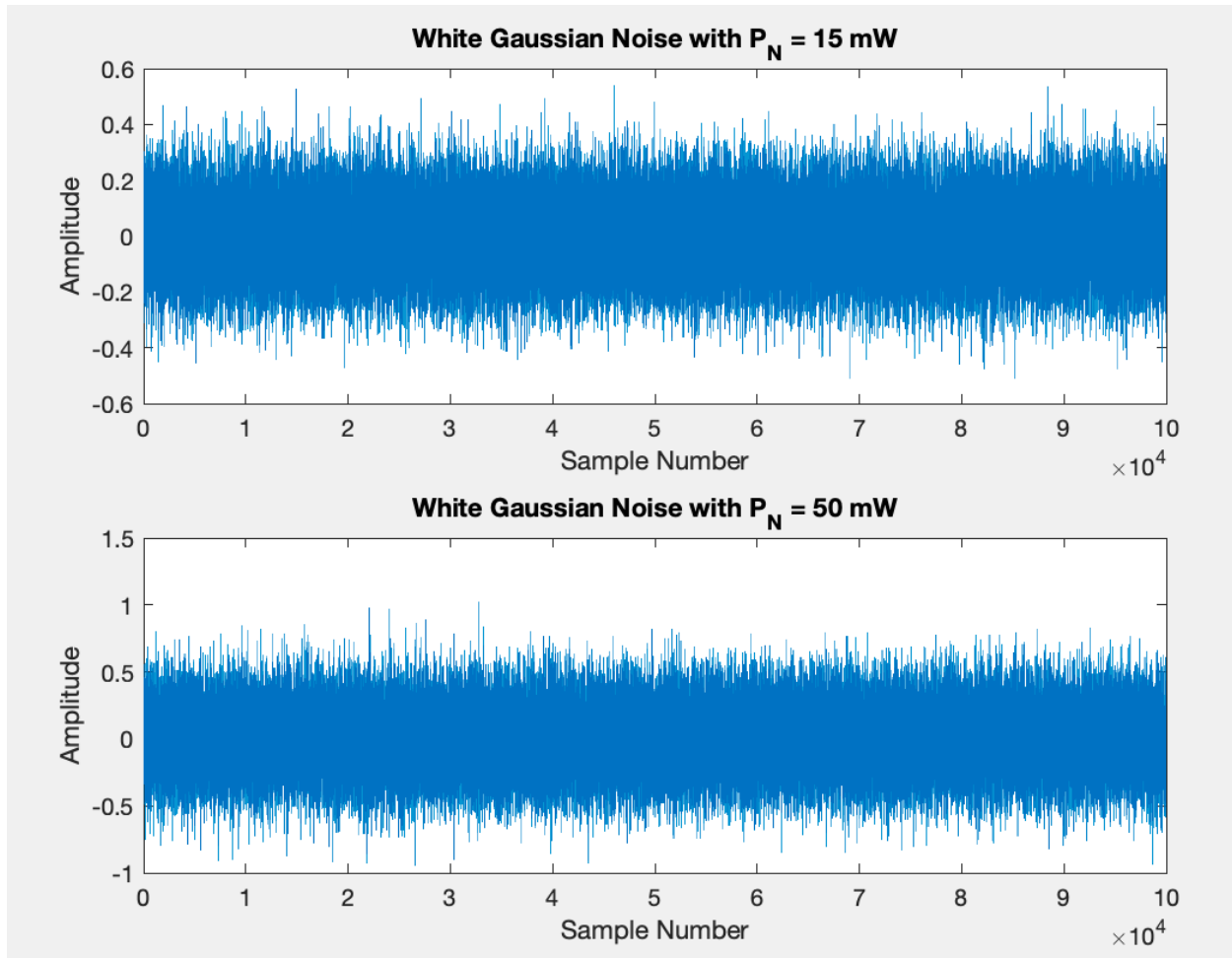


PART 1:



```
>> ECE4700_FinalProjectTesting  
Actual power of first noise signal: 0.014906 W  
Actual power of second noise signal: 0.05018 W
```

The actual power values will vary each time the code is ran, since it is a random process. However, the more samples used for the plotting will decrease the standard deviation of the each value, yielding approximate values closer to the expected. 100,000 samples were used in the results shown above, which was also beneficial for more accurate results in proceeding steps.

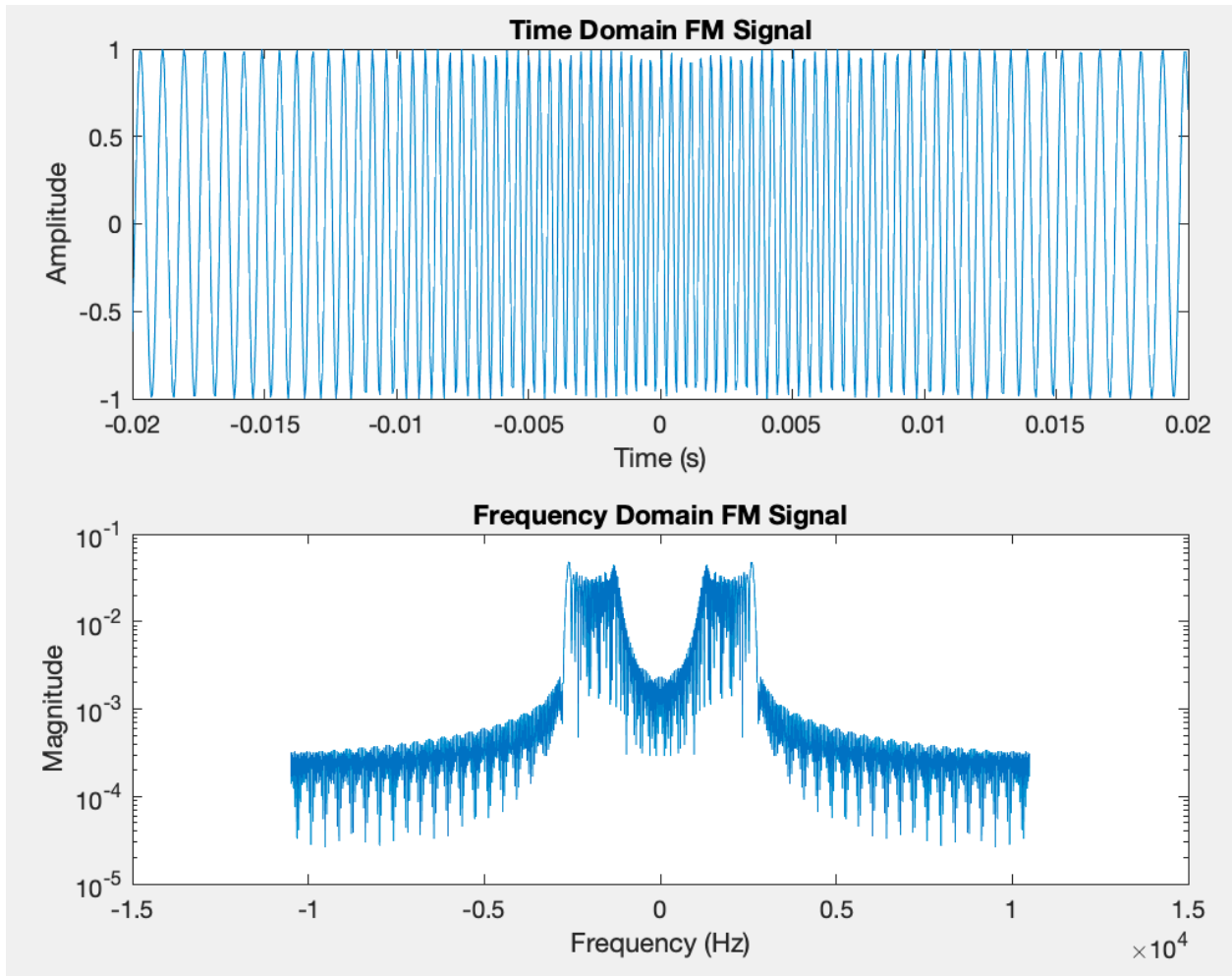
Code used for Part 1:

```
Editor - /Users/david/Desktop/ECE 4700/ECE4700_ComputerProject_Final.m
ECE4700_ComputerProject_Final.m x +
1
2 %ECE 4700 - Computer Project - David Baron-Vega
3 %Access ID: GF7068
4
5 %Part 1: Generating White Gaussian Noise at specified power levels.
6
7 % Noise power levels in mW
8 P_N1 = 15e-3; % 15 mW
9 P_N2 = 50e-3; % 50 mW
10
11 %Number of samples Needs to be tuned to get an accurate and precise
12 %result for power.
13 N = 100000; %can be tuned for more/less accurate and noisy signals.
14 %If N is bigger, standard deviation of output noise becomes much smaller
15
16
17 %Generating the WGN samples
18 n1 = sqrt(P_N1) * randn(N, 1);
19 n2 = sqrt(P_N2) * randn(N, 1);
20
21 %Plotting the WGN noise samples
22 figure;
23 subplot(2,1,1);
24 plot(n1);
25 title('White Gaussian Noise with P_N = 15 mW');
26 xlabel('Sample Number');
27 ylabel('Amplitude');
28
29 subplot(2,1,2);
30 plot(n2);
31 title('White Gaussian Noise with P_N = 50 mW');
32 xlabel('Sample Number');
33 ylabel('Amplitude');
34
35 %Computing the actual average power of the two noise signals
36 actual_power_n1 = mean(n1.^2);
37 actual_power_n2 = mean(n2.^2);
38
39 %Displaying the computed power values
40 disp(['Actual average power of first noise signal: ', num2str(actual_power_n1), ' Watts']);
41 disp(['Actual average power of second noise signal: ', num2str(actual_power_n2), ' Watts']);
42
43
```

It was important to calculate the actual power as I did above. Because WGN is a random, ergodic process, its ensemble mean is equal to its overall time average. Because we are generating random noise at a mu value of 0, the noise power is equal to the variance of the noise signal. This is why we square n1 and n2 above.

Part 2 Results:

Generating time-domain FM-modulated signal and frequency domain of signal using fft:



Code used:

```

61 %% PART 2: FM Modulation:
62
63
64 %Setting the signal's parameters
65 Ac = 1; %Carrier amplitude
66 kf = 200; %Frequency sensitivity (Hz/Volt)
67 fs = 21000; %Sampling frequency = 21KHz, much greater than fs > 2*B requirement.
68 fc = 1068; % 1000+ (my last 3 digits) are 068
69 t = -0.02:1/fs:0.02; %Time vector
70 ts = 1/fs; %Sampling interval
71
72 %Defining the band-limited message signal
73 mt = (2*sin(2*pi*20*t).^2)./(20*pi*t).^2;
74 mt(t == 0) = 1; %Correcting the sinc function at t = 0
75 figure;
76 plot(mt);
77 title('Message Signal m(t)');
78 xlabel('Time (s)');
79 ylabel('Amplitude');
80
81 %Integral of m(t) for FM
82 integral_mt = cumsum(mt)*ts;
83
84 %Creating the FM signal s(t)
85 st = Ac*cos(2*pi*fc*t + 2*pi*kf*integral_mt)
86
87 %Time domain results
88 figure;
89 subplot(2,1,1);
90 plot(t, st);
91 title('Time Domain FM Signal');
92 xlabel('Time (s)');
93 ylabel('Amplitude');
94
95 % Frequency domain representation
96 Lfft = 2^(nextpow2(length(t)) + 1); %Increasing the FFT resolution for more detail
97 S_fre = fft(st, Lfft);
98 S_fre = fftshift(S_fre)/Lfft; %Scaling the FFT output
99 freq = (-Lfft/2:Lfft/2-1)/(Lfft*ts); %Correcting frequency vector calculation, middle of graph is 0.
00
01 %Frequency domain results
02 subplot(2,1,2);
03 plot(freq, abs(S_fre));
04 title('Frequency Domain FM Signal');
05 xlabel('Frequency (Hz)');
06 ylabel('Magnitude');
07
08 %Setting the y-axis to use a logarithmic scale to better visualize the FFT output
09 set(gca, 'YScale', 'log');

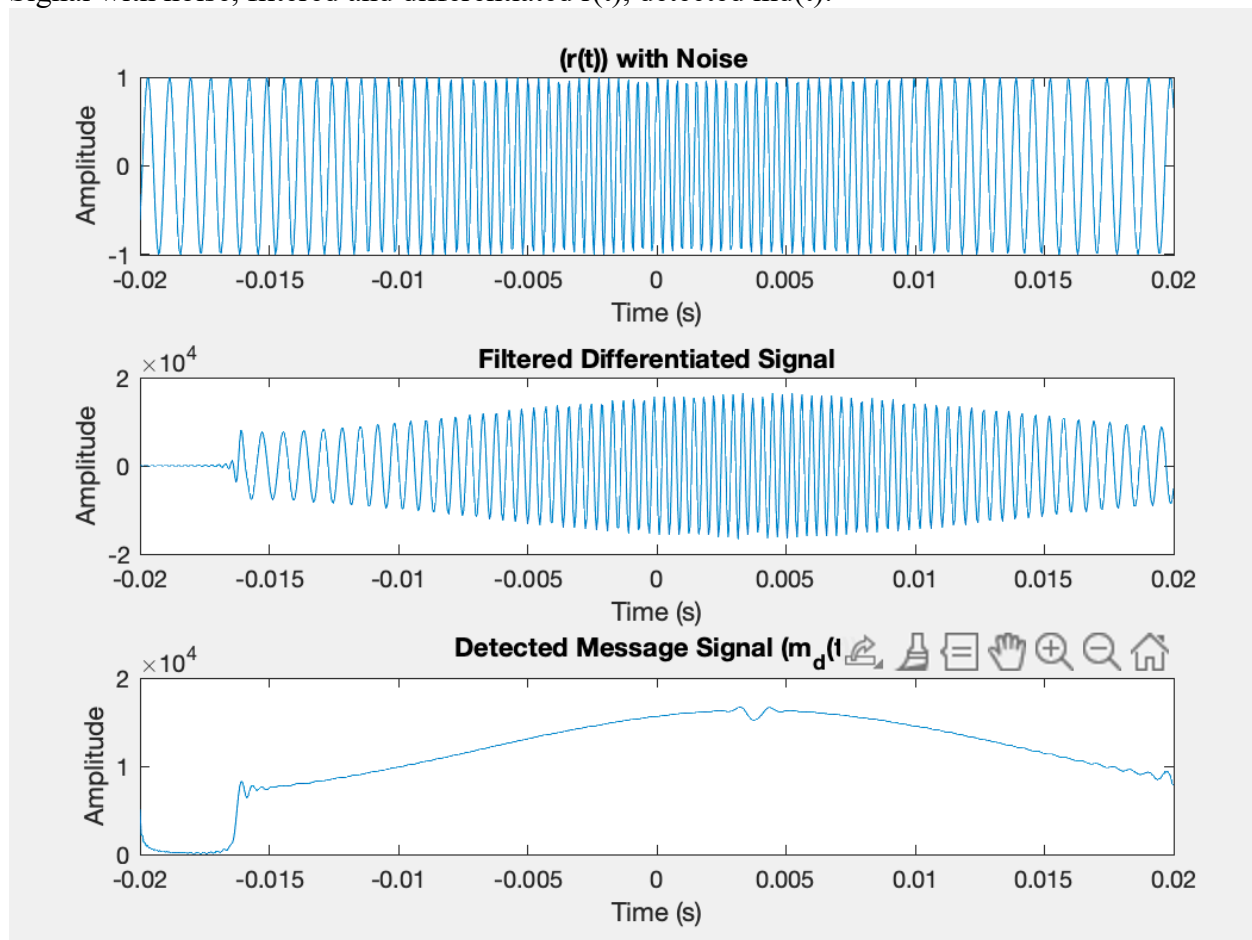
```

Comments:

Using the assigned value of kf, amplitude of 1, and an fc that is unique to my access id. A large fs and very small ts was helpful in producing clear results. It was also important to set the origin of the message signal to a non-zero value to produce the frequency-domain representation accurately.

PART 3:

Signal with noise, filtered and differentiated $r(t)$, detected $m_d(t)$:

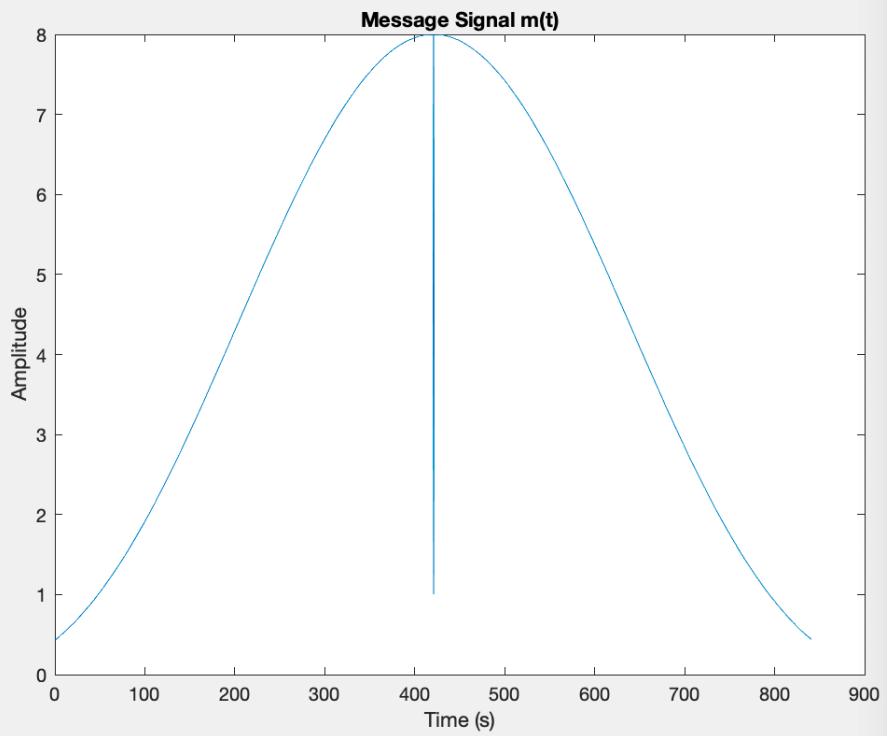
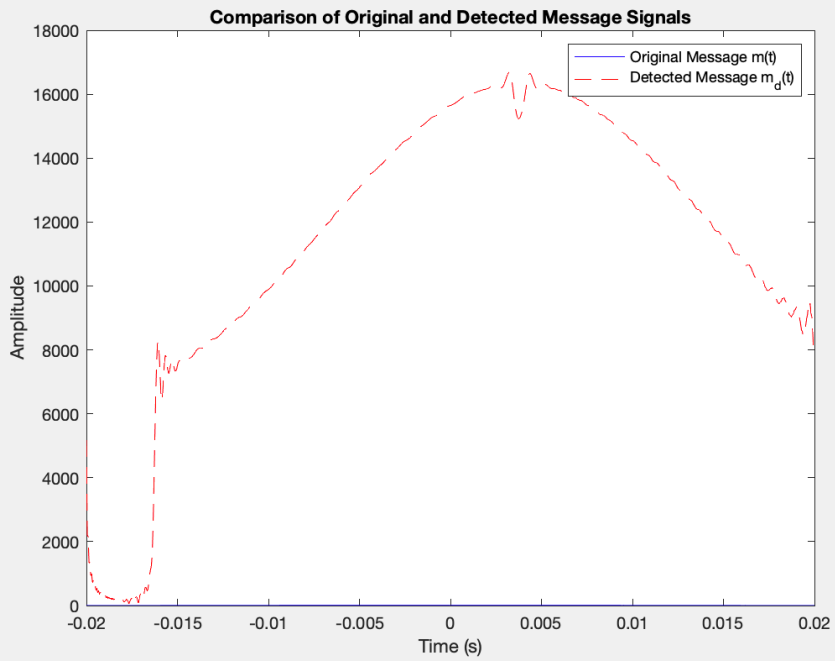


Comparing the original and detected:

The Amplitude of the detected is much, much, bigger! But the shape is fairly well retrieved.

Side by side comparison:

Ofcourse, the frequency of the retrieved signal is going to be higher. When this signal is differentiated, even after filtering performed before and after differentiated, the FM will come through as amplitude variations, so I believe this is what we would expect to see. If we needed the retrieved signal to be of lower amplitude, we would have to apply more filtering/limiting.



Code:

```
%%% PART 3: Noise in FM Channel and FM Demodulation

%Number of samples for noise should match the FM signal samples
N = length(t);
noise_power = 50e-3; %50 mW
n_t = sqrt(noise_power/fs) * randn(1,N); %Regenerating Noise signal:

%Creating the signal r(t):
r_t = st + n_t

%Time domain plot of r(t)
figure;
subplot(3,1,1);
plot(t, r_t);
title('(r(t)) with Noise ');
xlabel('Time (s)');
ylabel('Amplitude');
```

```

46 %Applying a limiter (optional)
47 %r_t = limiter_function(r_t);
48 %Applying a bandpass filter before differentiation
49 nyquist_freq = fs / 2;
50
51 %Lower and upper bounds for the bandpass filter must be strictly between 0 and 1!
52 %We can set a small value close to zero for the lower bound
53 lower_bound_normalized = (10/fs); %A small value close to zero but not zero
54 upper_bound_normalized = (4000/nyquist_freq); %Upper bound normalized and less than 1
55
56 bpf_before_diff = fir1(80, [lower_bound_normalized upper_bound_normalized]);
57 r_t_filtered = filter(bpf_before_diff, 1, r_t);
58
59
60
61
62 %Differentiate the signal, Check the orientation of the signal vector to
63 %add the necessary dimension,
64
65 %Kept bugging out here, idk why I need an extra zero in the array for this
66 %to differentiate tbh, one dimension was getting lost when differentiating
67 %I think.
68
69
70 diff_r_t = [diff(r_t_filtered), 0]; %Concatinate zero in the correct orientation
71
72 if isrow(r_t)
73     diff_r_t = [diff(r_t_filtered), 0]
74 else
75     diff_r_t = [diff(r_t_filtered); 0];
76 end
77 diff_r_t = diff_r_t / ts; %Scale by the sampling interval
78
79
80
81 %Applying another bandpass filter after differentiation
82 %Lower and upper bounds for the BPF between 0-1
83
84 lower_bound_normalized = (10/fs);
85 upper_bound_normalized = (4000/nyquist_freq);
86
87 bpf_after_diff = fir1(80, [lower_bound_normalized upper_bound_normalized]);
88 filtered_diff_r_t = filter(bpf_after_diff, 1, diff_r_t);
89
90
91 %Envelope detection to retrieve m_d(t)
92 md_t = abs(hilbert(filtered_diff_r_t));
93

```



```

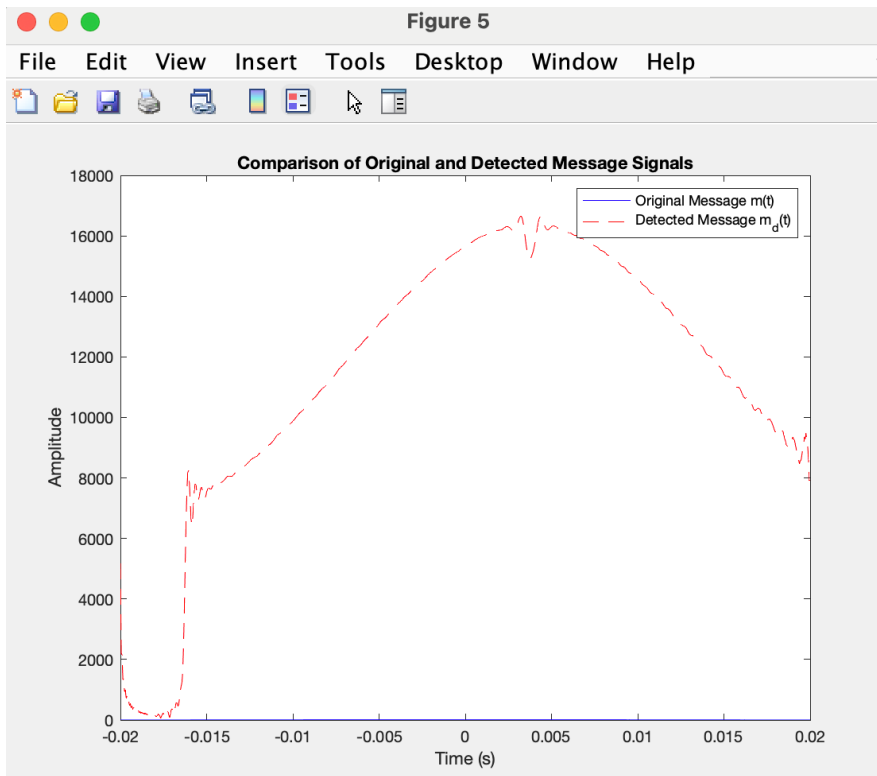
94 %Time domain plot of the filtered differentiated signal
95 subplot(3,1,2);
96 plot(t, filtered_diff_r_t);
97 title('Filtered Differentiated Signal');
98 xlabel('Time (s)');
99 ylabel('Amplitude');
00
01 %Time domain plot of the detected message signal m_d(t)
02 subplot(3,1,3);
03 plot(t, md_t);
04 title('Detected Message Signal (m_d(t))');
05 xlabel('Time (s)');
06 ylabel('Amplitude');
07
08 %Comparing m_d(t) with the original message signal m(t)
09 figure;
10 plot(t, mt, 'b', t, md_t, 'r--');
11 legend('Original Message m(t)', 'Detected Message m_d(t)');
12 title('Comparison of Original and Detected Message Signals');
13 xlabel('Time (s)');
14 ylabel('Amplitude');

```

I had to trial and error this part quite a bit with the filters, until my retrieved message resembled my original message better. Still, I couldn't lower the amplitude of the retrieved message enough as I would have liked. After differentiation, the vector used to plot the retrieved signal did not match the original length of the message, so I had to manually add values to the array in order to filter and then compute the retrieved message.

Part 4:

Comparing the original recovered message with new recovered messages with varying Kf values:



The comparison previously displays the comparison better, as the amplitude of the retrieved signal is much larger. The have the most similar shape when K_f is approximately 250. Anything beyond 400-500 for a K_f value already shows signs of overmodulation/sampling.

Code used:

```

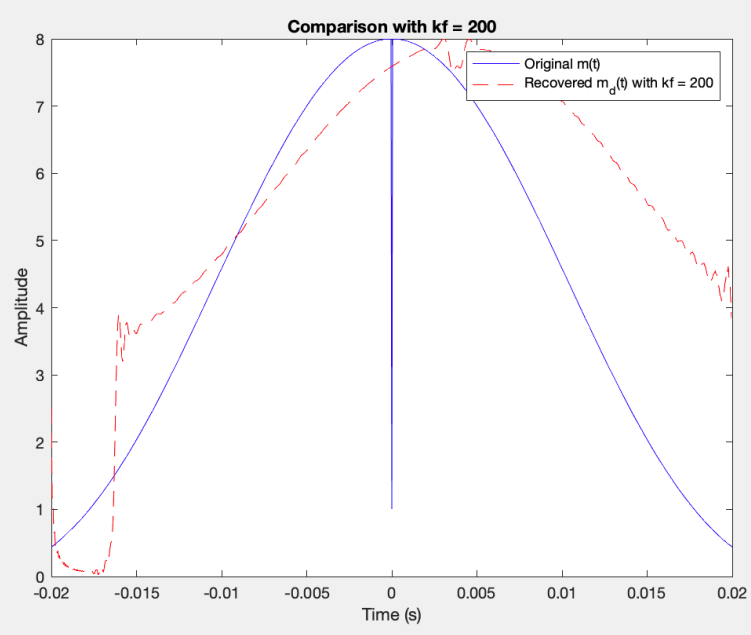
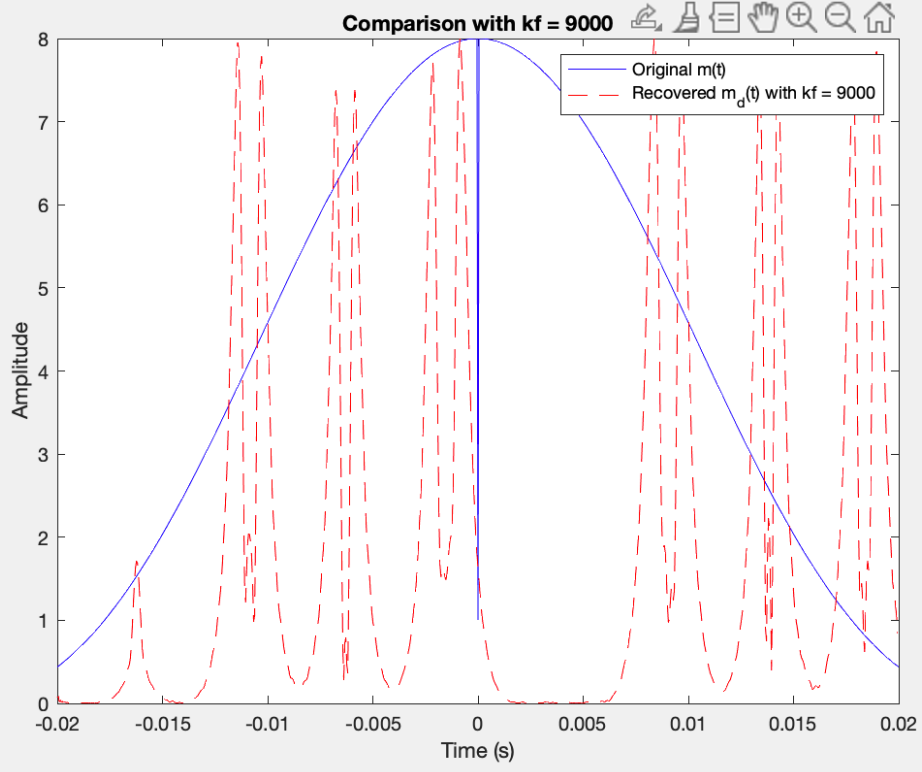
15
16 % Part 4: Optimizing md(t) by modifying kf:
17
18 %Setting kf values and initializing MSE storage
19 kf_values = [10, 200, 9000]; %Example values including one for over-modulation
20 mse_values = zeros(size(kf_values));
21 optimal_mse = inf;
22 optimal_kf = 0;
23
24 %Defining filters outside the loop:
25
26 nyquist_freq = fs / 2;
27 lower_bound_normalized = (10/fs);
28 upper_bound_normalized = (3600/nyquist_freq);
29 bpf_before_diff = fir1(100, [lower_bound_normalized upper_bound_normalized]);
30
31 %Loop over each kf value
32 for i = 1:length(kf_values)
33     kf = kf_values(i); %Current value of kf
34
35     %FM Modulation with new kf value
36     integral_mt = cumsum(mt) * ts; %Recalculating integral with new kf
37     st = Ac * cos(2*pi*fc*t + 2*pi*kf*integral_mt); %new FM signal
38
39     %Generating noise of same power 50mW and to match the FM signal samples
40     n_t = sqrt(noise_power/fs) * randn(1, length(t));
41
42     %Creating the noisy received signal r(t)
43     r_t = st + n_t;
44
45     %Applying the bandpass filter before differentiation
46     r_t_filtered = filter(bpf_before_diff, 1, r_t);
47
48     %Differentiating the signal
49     diff_r_t = [diff(r_t_filtered), 0];
50
51     %Applying a low-pass filter after differentiation
52     B_m = 4000;
53     bpf_after_diff = fir1(80, (B_m*2) / nyquist_freq); %Low-pass filter parameters
54     filtered_diff_r_t = filter(bpf_after_diff, 1, diff_r_t);
55
56     %Envelope detection to retrieve m_d(t)
57     md_t = abs(hilbert(filtered_diff_r_t));
58
59     %Scaling the envelope-detected signal to match the amplitude of the original message
60     scale_factor = max(mt) / max(md_t); %scaling factor
61     md_t_scaled = md_t * scale_factor;
62
63     %Calculating the Mean Squared Error for optimization
64     mse_values(i) = immse(mt(1:end-1), md_t_scaled(1:end-1));
65
66     %Checking if this kf is better
67     if mse_values(i) < optimal_mse
68         optimal_mse = mse_values(i);
69         optimal_kf = kf;
70     end
71
72     %Plotting the recovered message signal for current value of kf
73     figure;
74     plot(t, mt, 'b', t(1:end-1), md_t_scaled(1:end-1), 'r--');
75     legend('Original m(t)', 'Recovered m_d(t) with kf = ' + string(kf));
76     title(['Comparison with kf = ' + string(kf)]);
77     xlabel('Time (s)');
78     ylabel('Amplitude');
79 end
80
81 %Displaying the best kf value calculated in the above loop:
82 disp(['The best value of kf for FM demodulation is ' + string(optimal_kf)]);

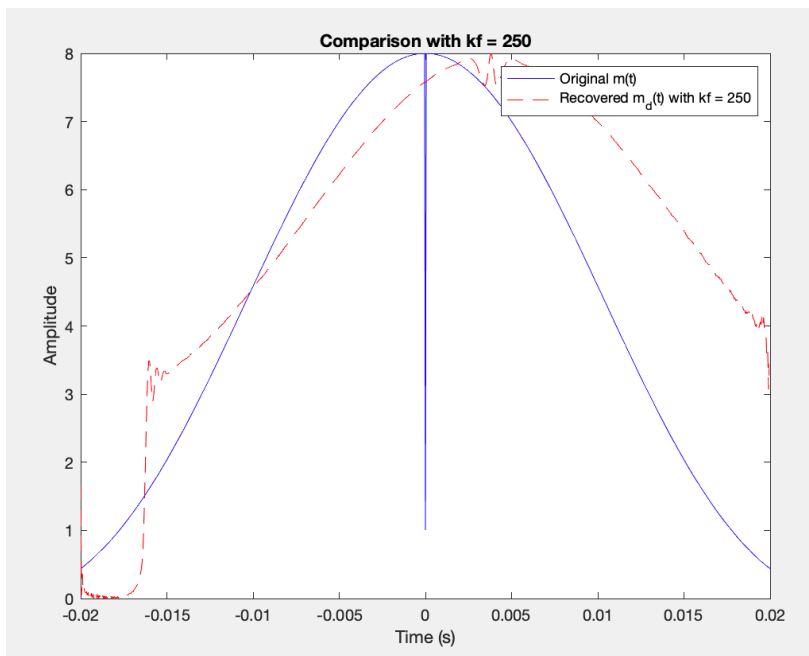
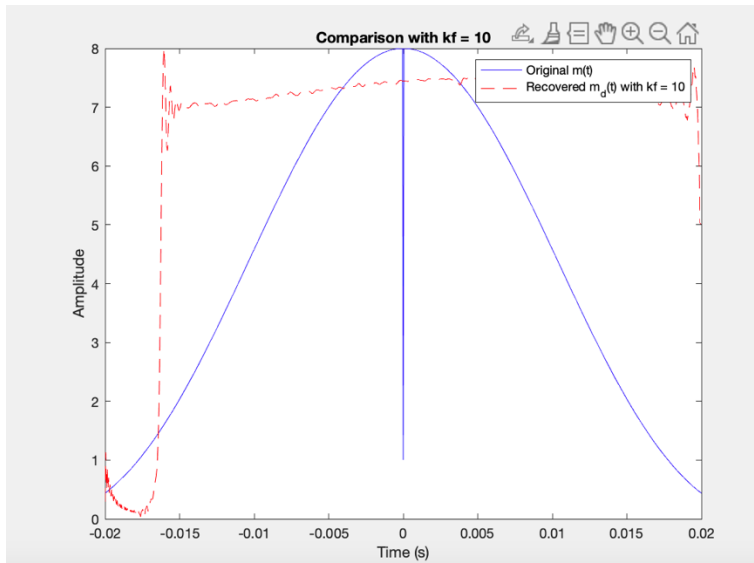
```

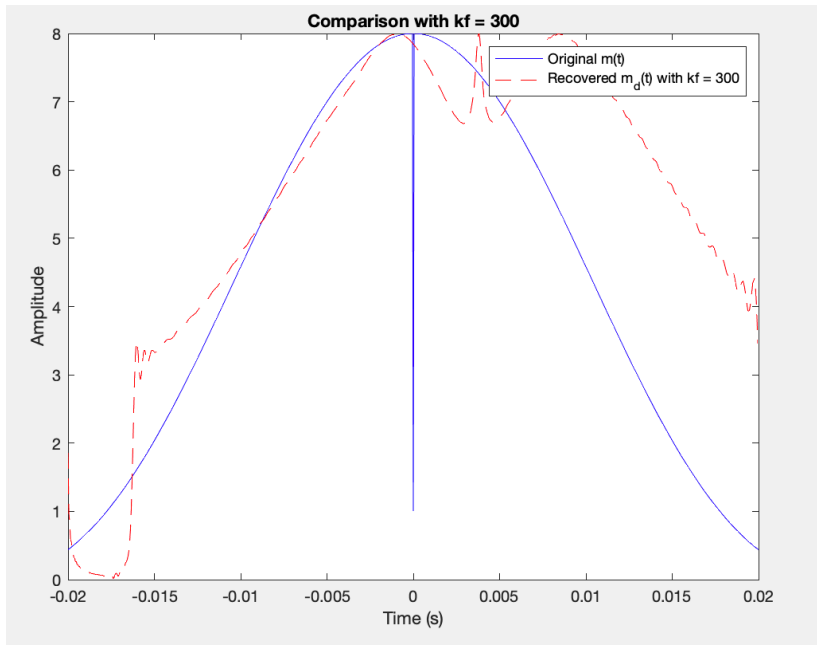
Note: I provided examples of many different K_f values used, which helped to visualize the effect of under and over modulating the signal.

Further discussion of K_f :

The value of K_f in an FM system controls the modulation index, and how much the signal's frequency changes. If K_f is too low, the signal can be easily messed up by the noise, but if it's too high, it will use too much bandwidth and cause overmodulation, picking up high frequency disturbances. Finding the right K_f is about making the signal strong against noise without taking up unnecessary bandwidth. The best K_f gives you a clearer retrieved signal that has an ideal SNR.







From the graphs above, we can once again see that a Kf of approximately 250-300 seems to be the best fit for our case.